SUBJECT PRESENTATION FORM

| Subject name | NUMERICAL ANALYSIS |
|----------------------|--|
| Field of study | Civil Engineering |
| Main field of study | Civil Engineering |
| Subject code | 41322008 |
| Subject main teacher | Prof. Adrian CHISALITA, MSc(Eng), BSc(Math), PhD |
| Collaborators | |
| | |
| Department | Structural Mechanics |
| Faculty | Civil Engineering (Construcții) |

| Sem. | Type of subject | Course | Appl | licati | ons | Course | Ap | plica | tions | Individual Study | S I | | Type of examination |
|------|-----------------|----------------|------|--------|---------------------|--------|----|-------|-------|---------------------|-----|---|------------------------|
| | | [Classes/week] | | | [Classes/semester.] | | | LOJ | Cre | | | | |
| | | | S | L | Р | | S | L | Р | | | • | |
| 3 | Fundamental | 1 | - | 1 | • | 14 | - | 14 | - | 50 | 78 | 3 | Exam |

Prerequisites: Differential Calculus; Fortran 90/95 programming language.

Theoretical knowledge, (What the students must know)

Aim: An introduction to Scientific Computation:

Applied Numerical Analysis, with problems solved on computer. Achieved skills: (What they can do)

The student is supposed to be able to handle most of numerical methods for solving equations; and, be _ able to analyze the accuracy and the stability of a numerical method.

At the same time, the student has to manage the use of library routines for building a project in order to solve a computational problem.

Achieved abilities: (What types of equipments and instruments they know how to use)

- To use a PC with Windows OS;
- To use the development environment of MS Visual Studio and CVF (Compaq Visual Fortran). _

| A. | Course (course titles +curriculum) |
|-----------|--|
| 1 | Object of Numerical Analysis: |
| | Object. Problem conditioning, condition number. Algorithm stability. Conclusions regarding problem |
| | conditioning and algorithm stability. |
| | Computer representation of numbers: |
| | Integers. Reals, floating-point representation: Representation models (scientific; binary computer). Format |
| | structure; IEEE Formats. |
| 2 | Computer representation of numbers –IEEE Formats: |
| | Special values; Representation range. |
| | Computer representation of numbers – Rounding error measure: |
| | ULP; machine-ɛ; Unit rounding error. |
| | Errors, sources and propagation: |
| | Error; Relative error; Significant digits. Error sources. Rounding error. Truncation case. Examples for base |
| | $\beta = 2.$ |
| 3 | Errors, sources and propagation – Error propagation: |
| | Propagated error. Multiplication; Division; Function evaluation. Loss of signification error. Addition and |
| | subtraction. Propagation of errors in a sum. |
| | Nonlinear equations: |
| | Method and method analysis; Order of convergence. Linear convergence. |
| 4 | Roots of an equation $f(x) = 0$: |
| | Bisection method. Secant method. Newton method; Error estimation; Comparison with Secant method. |
| | Fixed-Point method: |
| | Method. Convergence (contractive mapping). Geometrical interpretation. |
| 5 | Fixed-Point method: |
| | Method. Convergence (contractive mapping). Geometrical interpretation. Higher order Fixed-point methods. |
| | Error evaluation. Explicit Fixed-point procedures. The stationary process. |
| | Multiple roots of equation $f(x) = 0$: |
| | Problems. Newton method and Modified Newton method. |
| | Root of a polynomial: |
| | Polynomial evaluation; Deflation; Newton method for polynomials. Algorithm. Stability of the roots. |
| | Complex roots (elements). |

| 6 | Systems of non-linear equations: |
|---|--|
| | Definitions. Vector & Matrix norm. |
| | Fixed-point method. Convergence. Second order convergence. Practical iteration scheme. Explicit fixed- |
| | point procedure: Iteration with constant matrix A (updated). |
| | Newton method; Convergence; Practical iteration scheme. Newton-like methods. |
| 7 | Linear systems of equations: |
| | General considerations. |
| | Gauss elimination. Pivoting. Number of operations. Matrix inversion. |
| | LU decomposition. Direct evaluation of LU factors, methods. |
| | Cholesky method. |
| | Solution stability and error analysis: Condition number. Well- and ill-conditioned matrices |
| | |

| B1. | B1. Applications – WORKS (list of works, seminar works, contents of the year end project) | | | | |
|------------|---|--|--|--|--|
| 1 | Developer Studio Recall; Project structure; Building a project. Use of ANA Library. | | | | |
| | Algorithm stability (Bessel function direct and recursion computation) | | | | |
| 2 | Computer representation of numbers. Bitview utility. Special values. ULP; machine-&; Unit rounding error. | | | | |
| 3 | Errors. Bisection method. Secant method. | | | | |
| 4 | Newton method. Fixed-point method; Stationary process. | | | | |
| 5 | Roots of polynomials; Stability of the roots. Non-linear systems: Fixed-point method. | | | | |
| 6 | Non-linear systems: Newton method. Linear systems: Gauss. | | | | |
| 7 | Linear systems: Matrix inversion; LU; Cholesky. Condition number. | | | | |

| B2. Laboratory room (Room/surface, address) 304/58m ² , street Daicoviciu no.15, Tower Building, 3 rd floor. | | | | | |
|---|--|----------------------|--|--|--|
| Equipment | Equipment description | Year of purchase | | | |
| Computers Room 304: 14 pcs. | Computer: PC- Processor Pentium IV/3GHz/Mem.1024MB/ HDD 200GB/DVD-RW/Monitor TFT 19"/Keyboard & Mouse; | 2006 | | | |
| Software | MS Windows XP Professional, SP2 MS Office 2003 Compaq Visual Fortran 6.6C | 2005 2003 2001 | | | |

C. Individual study (topics of the bibliographical studies, summarized materials, projects, applications etc.)

- 1. Fortran 90/95 programming.
- 2. ANA sources & Examples.
- 3. Computer representation of numbers.
- 4. Exam Problem.

| Structure of | Course | Solving | Training, | Time | Bibliographical | Total number of classes |
|--------------|--------|-----------|--------------|--------------|-----------------|-------------------------|
| the | study | homework, | applications | allotted for | supplementary | for individual study |
| Individual | | labs, | | examinations | study | |
| study | | projects | | | | |
| No. of | 21 | 21 | 0 | 1 | 7 | 50 |
| classes | | | | | | |

D. Teaching methods and strategies

1. Course: Lectures.

2. Laboratory: Computer work, problem solving. Based on ANA Library & ANA User's Guide.

3. Exam Problem: One problem (randomly chosen) is given to each student at Lab #6, to be solved and be presented at the end-of-semester exam. The list of Problems is posted on ftp.utcluj.ro.

Bibliography

- 1. Chisalita A., "Numerical Analysis", UTC-N, 2002.
- 2. Chisalita A., "ANA Numerical Analysis Library (source code)", UTC-N, 1991-2009.
- 3. Chisalita A., "ANA User's Guide", UTC-N, 2008.
- 4. Atkinson K.E., "An Introduction to Numerical Analysis", John Wiley & Sons, N.Y., 1978
- 5. Atkinson K.E., "Elementary Numerical Analysis", 2nd edition, John Wiley & Sons, N.Y., 1993
- 6. Curtis F.G., "Applied Numerical Analysis", Addison-Wesley Publishing Company, Inc., 1978
- 7. Isaacson E., and Keller H.B., "Analysis of Numerical Methods", John Wiley & Sons, N.Y., 1966
- 8. Kincaid D., and Cheney W., "Numerical Analysis", 2nd edition, Brooks/Cole Publ. Co., 1996
- 9. Ralston A., and Rabinowitz Ph., " A First Course in Numerical Analysis", McGraw-Hill, Inc., 1978

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- 10. "Compaq Visual Fortran Language Reference Manual", 2001
- 11. "Compaq Visual Fortran Programmer's Guide", 2001
- "Intel Fortran Compiler 11.1 User and Reference Guide", 2009-2010
 "IMSL Mathematical and Statistical Libraries", Compaq Visual Fortran 6.6, IMSL Help, 1999.
- 14. "High-Precision Software Directory", 2010, http://crd.lbl.gov/~dhbailey/mpdist/

| Examination and grading procedure | | | | | |
|-----------------------------------|--|--|--|--|--|
| Examination procedure | Oral Examination. | | | | |
| | 1. One Theoretical Question: picked by the student from a lot of questions. | | | | |
| | The list of Theoretical Questions is posted on <u>ftp.utcuj.ro</u> , the last day of the | | | | |
| | semester. | | | | |
| | 2. One Problem: pre-solved and presented (on computer). | | | | |
| Components of the grade | 1. Theory Mark; 2. Problem mark; 3. Up to 1 point Bonus, for Lab attendance | | | | |
| | (Bonus = Lab attendance/7). | | | | |
| Formula for calculating | Final mark = $(\text{Theory mark} + \text{Problem mark})/2 + \text{Bonus} - \text{if applicable}.$ | | | | |
| the grade | Condition for passing: Each of Theory mark and Problem mark be ≥ 5 . | | | | |
| | The bonus is granted at the 1 st attendance to the exam, and only if the passing condition is | | | | |
| | fulfilled. | | | | |

Subject coordinator, Prof. Adrian CHISALITA